Incorporating geostationary lightning data into a radar reflectivity based hydrometeor retrieval method: An observing system simulation experiment

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**Abstract**

A retrieval method for deriving the hydrometeor mixing ratio within mesoscale convective system (MCS) is presented in this study. The hydrometeor retrieval method was designed to incorporate the flash extent densities (FED) data from the Feng-Yun-4 geostationary satellite into the S-band radar reflectivity ($Z_{\text{fl}}$) and ambient temperature ($T_{\text{fl}}$) data-based hydrometeor retrieval method. Total lightning data are utilized to better discern regions containing graupel and snow in clouds. In the quantitative estimation of rain mixing ratio, different intercept parameters are used for different ranges of $Z_{\text{fl}}$ and different estimated precursors of raindrop in cold-cloud microphysical processes (i.e., graupel and snow aggregate). The hydrometeor retrieval method was evaluated through an observing system simulation experiment (OSSE) in which the pseudo-input-data for the hydrometeor retrieval (i.e., the FED, $Z_{\text{fl}}$ and $T_{\text{fl}}$ data) were obtained from the cloud-scale (1-km) simulation of an MCS using explicit electrification implemented within the Weather Research and Forecasting model. By incorporating the FED data as an additional input data source into the $Z_{\text{fl}}$ and $T_{\text{fl}}$ based hydrometeor retrieval method, the hydrometeor retrieval accuracy was improved. The hydrometeor retrievals were then assimilated into the model using the Real-Time Four-Dimensional Data Assimilation (RTFDDA) system. Assimilating more accurate hydrometeor fields slightly improved the analyses and forecasts of convective precipitation in the test MCS case. The improvement could be due to the more accurate hydrometeor analysis, which further affected the strength of the cold pool and gust front.

**Keywords:** Lightning, Hydrometeor retrieval, Data assimilation, Numerical weather prediction, Observing system simulation experiment

1. Introduction

The retrieval of hydrometeor within convective clouds is useful to provide a more accurate estimate of latent heat release and to improve hydrometeor analyses for the initialization of convection-allowing numerical weather prediction (NWP) models, among other applications. These applications motivated several studies aimed at developing and testing hydrometeor retrieval methods (e.g., Dawson and Xue, 2006; Hu and Xue, 2007; Kain et al., 2010; Ziegler, 2013; Xue et al., 2014).

Owing to its high spatial and temporal resolution, weather radar remains the primary data source for hydrometeor retrieval. Previous studies have shown that polarimetric radars, which provide a variety of variables (e.g., reflectivity $Z_{\text{fl}}$, differential reflectivity $Z_{\text{dr}}$, specific differential phase $K_\text{dp}$, and correlation coefficient $\rho_{\text{HV}}$), have the ability to identify bulk hydrometeor types of convective clouds and improve the quantitative estimate of liquid water content (LWC) and ice water content (IWC; e.g. Vivekanandan et al., 1999; Straka et al., 2000; Zrnić et al., 2001).

For areas solely within the range of non-polarimetric radars, reflectivity ($Z_{\text{fl}}$) and temperature ($T_{\text{fl}}$) based hydrometeor retrieval methods have been developed by several investigators (e.g., May and Keenan, 2005; Hu et al., 2006; Lerach et al., 2010). The single $Z_{\text{fl}}$ threshold (e.g., 32 dBZ c.f. Lerach et al., 2010; Pan et al., 2016) is often used to classify the graupel-dominated regions and snow aggregates-dominated regions above the freezing level. Because the possible ranges of $Z_{\text{fl}}$ for graupel and snow aggregates partially overlap (i.e., the $Z_{\text{fl}}$ range of graupel and snow aggregates are typically 25–50 dBZ and 0–35 dBZ, respectively; Straka et al., 2000), single $Z_{\text{fl}}$ threshold could introduce uncertainty in distinguishing the graupel-dominated versus snow aggregates-dominated regions. Cazenave et al. (2016) tested the...
It can be inferred that the sensitivity of the classification of graupel and snow aggregates-dominated regions from 8% and 32.9% to 13.1%–3 dBZ changed the respective percentages of graupel-dominated regions and ice crystals in the presence of supercooled water, known as riming mechanism in thunderstorms arises from elastic collisions between graupel based hydrometeor retrieval method (include reference here). Research based on laboratory experiments (e.g., Reynolds et al., 1957; Takahashi, 1978; Saunders et al., 1991;) and field observations (e.g., Dye et al., 1986; Lang et al., 2004; Qie et al., 2005a, 2005b, 2009; MacGorman et al., 2005, 2008). Lightning discharge, which is a by-product of electrification and charge, is thus closely related to graupel content (e.g., Goodman et al., 1988; Carey and Rutledge, 1996; Fierro et al., 2006). Based on field observations, researchers found that the majority of lightning initiation occurs within or close to regions containing graupel (e.g., Bruning et al., 2007; Lund et al., 2009; Ribaud et al., 2016). Additionally, studies found that the regions without graupel (e.g., pure snow aggregates regions) are characterized by weak electric fields and lightning activity (Ribaud et al., 2016; Takahashi et al., 2017). These findings highlight the promising aspect of lightning data for indicating regions containing graupel.

Owing to recent developments of lightning detection techniques, lightning data have been used as a proxy for rainfall (e.g., Alexander et al., 1999; Chang et al., 2001; Pessi and Businger, 2009), water vapor content (e.g., Fierro et al., 2012, 2014, 2015, 2016) and hydrometeor mixing ratio (e.g., Qie et al., 2014; Wang et al., 2017). China recently launched the Feng-Yun-4 (FY-4) geostationary satellite (Yang et al., 2016). One of the instruments aboard FY-4 is the Lightning Mapping Imager (LMI), which is able to detect total lightning (i.e., in-cloud plus cloud-to-ground flashes) over China and its adjacent regions with a spatial resolution of about 8-km at nadir with a detection efficiency nearing 90-95% in real time (Yang et al., 2016). Most operational weather radars in China, however, are non-polarimetric, which imposes a stringent limitation for identifying graupel and snow aggregates. In this work, we demonstrate that the lightning data provided by the FY-4 geostationary satellite may, in some circumstances, help to improve the accuracy of the non-polarimetric radar based hydrometeor retrieval within mesoscale convective systems (MCs).

This study presents a hydrometeor retrieval method, which incorporates the lightning data from the FY-4 geostationary satellite as an additional input data source into the Z₀ and T based hydrometeor retrieval method. The hydrometeor retrieval method was evaluated via an observing system simulation experiment (OSSE). The impacts of the hydrometeor retrieval method on the short-term forecasts of an MCS at convection-resolving scale (1 km × 1 km) were evaluated through the use of the National Center for Atmospheric Research (NCAR) Real-Time Four-Dimensional Data Assimilation (RTFDDA) system.

2. Case description and model setup

2.1. Brief description of the severe convective event

An MCS, which took place in the North China Plain on 13 June 2010 was selected as the OSSE case. The MCS initially developed over the northwestern Hebei province around 0500 UTC and gradually moved southeastward toward Beijing around 1200 UTC. The MCS dissipates shortly before moving over the Bo Sea by 1800 UTC. The severe convective event lasted for > 15 h. It was influenced by a deep low (996 hPa) situated over eastern Inner Mongolia. Convective available potential energy (CAPE) exceeded 2200 J/kg throughout much of Hebei, Beijing and Tianjin during this time, while convective inhibition (CIN) was overall weak (approximately ~30 to ~200 J/kg), indicating an environment favorable for severe convection.

2.2. Model setup

The numerical model used for this work is the Weather Research and Forecasting - Electrification (referred to as E-WRF; Mansell et al., 2005; Fierro et al., 2013) model. The simulation domains included two nested grids (Fig. 1). The horizontal grid spacings were 9 km, 3 km (i.e., convection-allowing scale) and 1 km (i.e., cloud-resolving scale) for each of the three domains, respectively. Hydrometeor retrieval and data assimilation were only performed in the innermost, cloud-resolving domain. Two-way nesting between parent and inner nests were activated, so the impact of data assimilation can feedback from the innermost cloud-resolving domain to its parent domains. Each domain features 43 vertical eta levels with a model top set at around 50 km. The “true simulation” used the ERA-Interim reanalysis produced by the European Centre for Medium-Range Weather Forecasts (ECMWF; Dee et al., 2011) as initial and lateral boundary conditions. The simulations were initialized at 0600 UTC, 0700 UTC, 0900 UTC for the D01, D02 and D03, respectively, and were ended at 0000 UTC, 14 June 2010. The initial fields for the nested domain were interpolated from their parent domain. The MCS was well captured by the innermost cloud-resolving domain (i.e., D03) during the entirety of the simulation (i.e., ~15 h).

The physical schemes employed in this study included the NSSL double-moments bulk microphysics (Ziegler, 1985; Mansell et al., 2010a,b), the Noah land surface model (Chen and Dudhia, 2001), the Mellor–Yamada–Janjic turbulence kinetic energy (TKE) scheme for the planetary boundary layer (Janjic, 1994), and the Rapid Radiative
Transfer Model GCMs (RRTMG) for shortwave and longwave radiation (Jacono et al., 2008). The Grell-Freitas convective parameterization scheme (CPS; Grell and Freitas, 2013) was only activated in the parent domain (D01).

3. Methods

3.1. Simulated observations

The pseudo-LMI flash extent density (FED) observations were simulated using explicit electrification and lightning physics (Mansell et al., 2005; Fierro et al., 2013) which are coupled with the NSSL double-moment bulk microphysics scheme within WRF (E-WRF). The flash origin density and FED are explicitly simulated by E-WRF, which resolves the three-dimensional field of charge and solves for the three components of the ambient electric potential and, thus, ambient electric field. For more details on E-WRF, the reader is invited to consult Mansell et al. (2005) and Fierro et al. (2013). The areal extents of the simulated flash origin density were found to be reasonably consistent with the observations from the Earth Networks Total Lightning Network (ENTLN; Fierro et al., 2013).

In this set of simulations, the Saunders and Peck Scheme (Saunders and Peck, 1998; Mansell et al., 2005) was selected as the non-inductive charging scheme; for breakdown, the vertical electric field profile of Dwyer, (2005) was employed; the screening layer parameterization was de-activated; the size of the discharge cylinders was set to 6-km; the fraction of the net charge removed/superposed within the cylinder volumes upon bulk discharge was set to 60%.

The simulated 1-km FED were accumulated over a 15-min period and centered around the radar sampling time. The pseudo-LMI FED at each 8-km pixel was generated by selecting the maximum 1-km FED within the 8-km pseudo-LMI pixel (Fig. 2). The 8-km FED obtained using this approach likely are underestimated, as multiple lightning channels will follow the distribution of graupel particles, and therefore, it is reasonable to expect that lightning initiation and propagation are introduced. The initiation and propagation of lightning is driven by the ambient electric field and electric potential, which are determined by the three-dimensional distribution of electric charge (e.g., Mansell et al., 2002, 2010; Tan et al., 2012; Gao and Stensrud, 2012; Pan et al., 2016). When a double-moment microphysics scheme is used, number concentration is allowed to vary independent of the mixing ratio, which can significantly improve the analysis of particle size distributions (PSD) and the computation of radar reflectivity. Cloud ice and cloud water were not considered when computing $Z_b$ due to their negligible contributions. It was assumed that the effect of the 0 °C layer bright band has been corrected during the quality control process and the observations of $Z_b$ were perfect. The $Z_b$ data were interpolated from the radar polar coordinate onto the 1-km, Cartesian grid of D03.

3.2. Identification of the dominant hydrometeor type

The hydrometeor retrieval algorithm presented here is based on algorithms for non-polarimetric radar developed by Lerach et al. (2010), Gao and Stensrud (2012) and Pan et al. (2016), which use the S-band $Z_b$ and $T$. In the hydrometeor retrieval method presented here, the FED data were combined with $Z_b$ and $T$ to identify the hydrometeor type and to determine the intercept parameters of raindrop when quantitatively estimating rain mass mixing ratio ($q_r$).

The hydrometeor categories in the retrieval method contain rain, graupel and snow aggregates. The category of snow aggregates here refers to aggregated-ice and the category of graupel refers to rimed ice and heavily rimed snow, which is consistent with the definition in most bulk microphysical parameterization (BMP) schemes and dual-polarimetric radar based hydrometeor retrieval algorithms. Hail is not classified, as hail and graupel are not always explicitly treated separately in microphysics schemes.

Before describing the hydrometeor retrieval method, the information regarding which regions of a storm are favorable for frequent lightning initiation and propagation are introduced. The initiation and propagation of lightning is driven by the ambient electric field and electric potential, which are determined by the three-dimensional distribution of electric charge (e.g., Mansell et al., 2002, 2016; Tan et al., 2014; Bruning and MacGorman, 2013; Wang et al., 2016). It is generally accepted that most of the electric charge in convective clouds is generated by the non-inductive mechanism, which requires the presence of graupel pellets. Therefore, it is reasonable to expect that lightning channels will follow the distribution of graupel particles, and graupel echo volume has been used as a proxy for lightning channel interactions with the ambient electric potential and, thus, ambient electric fields.

**Fig. 2.** Horizontal cross sections of (a) simulated FED fields in D03 (1 × 1 km$^{-2}$, 15 min$^{-1}$) and (b) the pseudo-LMI FED (8 × 8 km$^{-2}$, 15 min$^{-1}$).
density (i.e., the FED; Allen et al., 2016). As convection matures, some charged ice crystals and snow aggregates are advected rearward into the anvil or trailing stratiform region (e.g., Carey et al., 2005) allowing some lightning flashes to propagate beyond the graupel regions in the updraft core into regions where the charge density is sufficient for continued propagation of lightning (e.g., Carey et al., 2005). Lightning can also occur in MCS stratiform regions and anvils of mature storms where graupel contents are low (Kuhlman et al., 2009). However, the FED rates in such regions generally are noticeably lower than in the vicinity of updraft cores (Carey et al., 2005; Calhoun et al., 2013). It was thus assumed that regions where the FEDs are significantly smaller than the average FED over the entire convective cell (F_AVG), would more likely be characterized by low charge density regions consisting of charged snow aggregates advected from the non-inductive electrification regions. The following approach was devised to filter the FED in those regions.

(i) In the FED map (8 km × 8 km), we clustered convective cell by using the accumulated FED data within a 15-min interval. If a pixel with non-zero FED is connected with other pixels with non-zero FED value, they are grouped into the same convective cell.

(ii) Computing the average FED for each clustered convective cell within a time window of 15-min (F_AVG).

(iii) Filtering the pixels with large negative deviations of FED from F_AVG. In this study, the pixels with FED < 0.16F_AVG were filtered out. We use the relative values instead of the absolute values as the filter parameter is designed to prevent the low FED convective cells from being filtered out. Since this filter threshold is somewhat arbitrary, it is challenging to exactly filter the low charge density regions consisting of charged ice crystals and snow aggregates advected from the non-inductive electrification regions. More accurate calibration of this parameter needs to be investigated in future study using real FED observations from the FY-4 geostationary satellite.

In order to jointly use the FED and Z_0 data, the coverage of filtered 8-km FED was mapped onto the 1-km grid, i.e., if one 8-km pixel has a non-zero FED, all the 1-km pixels within that 8-km pixel will be assigned a non-zero FED value.

In the follow-on steps, graupel is classified in grid cells located in the cold cloud regions (T < 0 °C), when one of the following criteria is met:

(i) The grid cell lies within the filtered FED outlines and Z_0 > 25 dBZ.
(ii) The grid cell lies outside the filtered FED outlines and Z_0 > 35 dBZ.

Similarly, snow aggregate is classified as follows:

(i) The grid cell lies within the filtered FED outlines and the 0 dBZ < Z_0 < 25 dBZ.
(ii) The grid cell lies outside the filtered FED outlines and the 0 dBZ < Z_0 < 35 dBZ.

The philosophy behind the choice of these particular criteria is that the regions inside the filtered FED outlines are those most likely to contain graupel particles. Therefore, the Z_0 threshold used to differentiate between graupel and snow aggregates is set to the lower limit of the Z_0 range of graupel (25 dBZ). For a time period of 15-min, the regions outside the filtered FED outlines are relatively less likely to contain graupel particles. In this case, the Z_0 threshold used to differentiate between graupel and snow aggregates is set to the upper limit of the Z_0 range of dry snow aggregates (35 dBZ), as Z_0 hardly exceeds this threshold without the existence of graupel in cloud regions.

The in-situ observations indicated that the regions of pure graupel are rare, and most cold-cloud regions consist of pure snow aggregates or mixed graupel/snow aggregates (e.g. Sukovich et al., 2009). Therefore, in cold-cloud regions, the grid cells identified as being dominated by graupel are regarded as mixed graupel/snow aggregates regions, and the grid cells identified as being dominated by snow aggregates are regarded as pure snow aggregates regions.

Because graupel and snow aggregates could coexist in the melting layer, their threshold temperatures are extended below the freezing level, namely: up to 5 °C and 3 °C respectively. The remaining hydrometeor species below the freezing level is classified as rain.

3.3. Quantitative estimations of hydrometeor mixing ratio

For the regions only containing one class of hydrometeor (e.g., pure rain or pure snow aggregates), the mixing ratio was simply computed using the Z_r-q equations. When multiple species coexist in the mixed regions, the measured total equivalent reflectivity factor (Z_r, mm^6 m^-3) is partitioned and allotted to each hydrometeor species based on empirical observation results.

In the mixed graupel/snow aggregates regions, graupel and snow aggregates contribute to Z_r. The equivalent reflectivity factor of graupel (Z_{r,graupe}l) is computed as follows,

\[ Z_{r,graupe}l(i,j,k) = p \cdot Z_r(i,j,k) \]  

where 0 < p ≤ 1 is the fraction of the Z_r from graupel.

Because graupel has a larger terminal fall speed than snow aggregate, it is reasonable to expect that graupel and snow aggregates in the mixed graupel/snow aggregates regions show differences in their vertical distribution. The trapezoidal weighting functions corresponding to ambient temperature profile for graupel and snow aggregates, which were used in Zrnić et al. (2001), were employed to consider the vertical distributions of graupel and snow aggregates. The equivalent reflectivity factor of graupel that takes into account the vertical distribution of graupel (Z_{r,graupe}l) can be expressed as:

\[ Z_{r,graupe}l(i,j,k) = \frac{p \cdot W_{graupe}l(T(k))}{p \cdot W_{graupe}l[T(k)] + (1-p) \cdot W_{snow}[T(k)]} \cdot Z_r(i,j,k) \]  

where i, j, k represent the horizontal and vertical coordinate dimensions, T(k) is the ambient temperature profile, and W_{graupe}l[T(k)] and W_{snow}[T(k)] are the trapezoidal weighting functions (between 0 and 1) corresponding to ambient temperature profile for graupel and snow aggregates.

The equivalent reflectivity factor of snow aggregates (Z_{r,snow}) in the mixed graupel/snow aggregates regions is computed as follows:

\[ Z_{r,snow}(i,j,k) = \frac{(1-p) \cdot W_{snow}[T(k)]}{p \cdot W_{graupe}l[T(k)] + (1-p) \cdot W_{snow}[T(k)]} \cdot Z_r(i,j,k) \]  

In convective clouds, the fraction of graupel in the mixed graupel/snow aggregates regions varies from case to case. Here, we assumed p = 0.9 in the mixed graupel/snow regions. The upper limit of Z_{r,snow} was set to 10^{3.5} mm^6 m^{-3}, as the Z_r for snow aggregates hardly exceeds 35 dBZ (e.g., Straka et al., 2000). If the calculated Z_{r,snow} exceeded 10^{3.5} mm^6 m^{-3}, the grid cells were reallocated to graupel. The graupel mixing ratio (q_g) and snow aggregates mixing ratio (q_s) in the mixed graupel/snow aggregates regions were computed using Z_{r,q} relationships where Z_{r,graupe}l and Z_{r,snow} were determined.

In the melting layer, q_g and q_s were estimated using a linear function with their values at the cold-cloud regions used as the starting value. Because it was assumed that the effects of the bright band near the freezing level have been corrected during the quality control, the graupel and snow aggregates were assumed to be dry. The Z_{r,snow} in the melting layer was calculated after subtracting the Z_{r,graupe}l and Z_{r,snow}.

When using Z_r-q relationship to quantitatively estimate the hydrometeor mixing ratio, the PSD were assumed to be exponential shape (Eq. 4).

\[ N_r(D) = N_{0s} \exp(-\lambda_s D_s) \]
where \( x \) represents the hydrometeor species (i.e., graupel, snow aggregates, rain), \( N_f(D)\Delta D \) is the drop numbers per unit volume between diameters \( D \) and \( D + \Delta D \), \( \lambda_0 \) is the intercept parameter, which is the value of \( \lambda_0 \) for \( D = 0 \), \( \lambda_0 \) is the slope parameter, which is diagnosed as

\[
\lambda_0 = \left( \frac{\rho_i \pi N_{0r}^3}{\rho_q} \right)^{0.25}
\]

where \( \rho_i \) is the bulk density of hydrometeor, \( \rho \) is the air density, and \( q_r \) is the hydrometeor mixing ratio.

The intercept parameters and the densities of graupel and snow aggregates (Table 1) were assumed constant. Although this assumption was used in previous studies (e.g., Xue et al., 2006; Tong and Xue, 2008), it is important to highlight that there exist uncertainties in these assumptions, as the PSD varies significantly in space and time.

The relationship between the \( Z_\text{h} \) for rain computed using the double-moment microphysics parameters (i.e., mixing ratio and number concentration) and \( q_r \) were analyzed throughout the life cycle of a simulated MCS (Fig. 3). It was found that with the increase of \( Z_\text{h} \) rain, \( q_r \) tended to be overestimated when the intercept parameter of rain (\( N_{0r} \)) was set to \( 8 \times 10^6 \) m\(^{-4} \), which value has been widely used for representing raindrop PSD (e.g., Lin et al., 1983; Hong et al., 2004). When \( N_{0r} \) was set to \( 3 \times 10^6 \) m\(^{-4} \), such overestimation was partially alleviated (Fig. 3). This is consistent with past studies that the high \( Z_\text{h} \) regions are more likely to be associated with relatively low number concentrations, which is an indication of larger drop size (e.g., Schuur et al., 2001; Carlin et al., 2016). Cold rain processes contribute significantly to the total rainfall within MCS (e.g., Houze Jr, 1997). The other factor that affects raindrop size was found to be the precursor of raindrop in cold cloud microphysical processes (e.g., Waldvogel, 1974; Fabry and Zawadzki, 1995). In the case of equal \( Z_\text{h} \) value, raindrops resulting from the melting of snow aggregates tend to have a larger size than those which melted from graupel (e.g., Waldvogel, 1974).

Infused from these findings, \( N_{0r} \) was not assumed constant in this hydrometeor retrieval method.

(i) In the column where only snow aggregates exist above 0 °C:

\[
N_{0r} = \begin{cases} 
8 \times 10^6 \text{m}^{-4}; & 0 < Z_\text{h} \leq 35 \text{dBZ} \\
(43 - Z_\text{h}) \times 10^6 \text{m}^{-4}; & 35 < Z_\text{h} \leq 40 \text{dBZ} \\
3 \times 10^6 \text{m}^{-4}; & Z_\text{h} > 40 \text{dBZ}
\end{cases}
\]

(ii) Similarly, in the column where graupel exists above 0 °C:

\[
N_{0r} = \begin{cases} 
9 \times 10^6 \text{m}^{-4}; & 0 < Z_\text{h} \leq 35 \text{dBZ} \\
(44 - Z_\text{h}) \times 10^6 \text{m}^{-4}; & 35 < Z_\text{h} \leq 40 \text{dBZ} \\
4 \times 10^6 \text{m}^{-4}; & Z_\text{h} > 40 \text{dBZ}
\end{cases}
\]

Since the slope of the rain PSD is proportional to \( N_{0r} \), decreasing \( N_{0r} \) shifts the peak of raindrops PSD toward bigger drops. The best-fitted relationship between \( N_\text{ff} \) and \( Z_\text{h} \) was not derived using the model simulations, as such a relationship is sensitive to the microphysics scheme used.

4. Results

4.1. The evaluation of the hydrometeor retrieval method

To evaluate the effects of incorporating FED as an additional data source into the \( Z_\text{h} \) and \( T \) based hydrometeor retrieval method, two main experiments were devised namely, “FED-Z\text{h}T” wherein FED, \( Z_\text{h} \) and \( T \) are used in the hydrometeor retrieval and “Z\text{h}T” where only \( Z_\text{h} \) and \( T \) are used via the OSSE approach. For \( Z\text{h}T \), the thresholds used to identify hydrometeor types were the same as in Lerach et al. (2010), e.g., the snow aggregates and graupel were segregated using a fixed \( Z_\text{h} \) threshold of 32 dBZ.

The simulated FED, \( Z_\text{h} \) and \( T \) from the true simulation were used as the input data for FED-Z\text{h}T and \( Z\text{h}T \). The hydrometeor retrievals were performed every 15-min starting when the simulated MCS began to produce lightning at 1-h forecast. The retrieved hydrometeor mixing ratios (i.e., \( q_g \), \( q_s \), \( q_r \)) from the two different retrieval methods were compared to those from the true simulation. The evolution of the MCS in the true simulation is shown in Fig. 4.

In general, the regions of rain, graupel, and snow aggregates were reasonably well classified by \( Z\text{h}T \) (Fig. 5b,e). The areal extents of some graupel regions, however, were smaller than those in the true simulation (Fig. 5b), as \( Z_\text{h} \) of the regions consisting of small graupel particles might be < 32 dBZ, which was the threshold used to identify the graupel-dominated regions in the \( Z\text{h}T \). In FED-Z\text{h}T, a relatively lower \( Z_\text{h} \) threshold was employed in lightning regions for identifying areas containing graupel particles. Overall, this approach improved the graupel estimations (Fig. 5c,f). The snow aggregates regions where \( Z_\text{h} \) exceeded 32 dBZ were misidentified as graupel regions in \( Z\text{h}T \) (Fig. 5e). In FED-Z\text{h}T, the relatively higher \( Z_\text{h} \) threshold for identifying graupel was applied in the regions outside the filtered FED outlines, which reduced the misidentification of graupel (Fig. 5f). As a result, the retrieval biases of graupel in \( Z\text{h}T \) were alleviated in some cases in FED-Z\text{h}T (Fig. 6).

In convective clouds, in-situ observations from aircraft revealed that

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Table 1

A summary of the intercept parameters and bulk densities of each hydrometeor categories used in the hydrometeor retrieval method.

<table>
<thead>
<tr>
<th>Categories</th>
<th>Intercept parameter (m(^{-4}))</th>
<th>Density (kg m(^{-3}))</th>
</tr>
</thead>
<tbody>
<tr>
<td>Graupel</td>
<td>(3 \times 10^6)</td>
<td>400</td>
</tr>
<tr>
<td>Snow aggregates</td>
<td>(2 \times 10^7)</td>
<td>100</td>
</tr>
<tr>
<td>Rain</td>
<td>(8 \times 10^6) variable</td>
<td>1000</td>
</tr>
</tbody>
</table>

Fig. 3. Comparison of the \( Z_\text{h}-q_r \) equation (\( Z_\text{h} \) is converted to \( Z_\text{h} \) herein) for raindrops when assuming an exponential shape PSD (Eq. (4)) with different \( N_{0r} \) (dash curves) and \( q_r \) versus \( Z_\text{h} \) from rain (red dots) computed using the double-moment microphysics parameters throughout the life cycle of the simulated MCS. The formulae used to compute \( Z_\text{h} \) from rain with the double-moment microphysics parameters was the same as in the radar simulator coupled in the NSSL double-moments bulk microphysics scheme. The values of \( N_{0r} \) corresponding to each curve are marked with colored font. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)
supercooled raindrops can often be lofted above 0 °C up to -10 °C by sufficiently strong updrafts (e.g., Brandes et al., 1995; Bringi et al., 1997). This observation was corroborated by the discovery of “ZDR columns” above 0 °C with polarimetric radars (e.g., Conway and Zrnić, 1993). In the true simulation, it was found that the raindrops were lofted above 0 °C, while the raindrops above 0 °C were neglected in both Z0,T and FED-Z0,T, which resulted in an underestimation of qr above 0 °C (Fig. 6). Past studies found that supercooled raindrops between 0 °C and -10 °C typically have large size (e.g. Hubbert et al., 1998; Carlin et al., 2016), and thus have a significant contribution to Z0. When raindrops were neglected above 0 °C, the Z0 contribution from the raindrops is allocated to graupel and snow aggregates, which resulted in overestimations of qg and qs where supercooled raindrops should exist (Fig. 6).

In the regions below 0 °C, the primary source of error in the retrieval of qr originates from the variations of raindrop size. In the Z0,T, a constant N0,r was used in the Ze-q retrieval equation for rain. This resulted in a noteworthy overestimation of qr in some regions (Fig. 6a,c) due to the existence of large size raindrops. By employing a variable N0,r to account for the variations of the raindrop size in different regions, the overestimation of qr retrievals were reduced (Fig. 6b,d).

To quantify the performance of FED-Z0,T, the equitable threat score (ETS, Clark et al., 2010) and frequency bias (BIAS) were computed for the retrievals of qg, qr, and qs from the FED-Z0,T and Z0,T, respectively. When computing the ETS and BIAS, the true simulation was regarded as the reference. The ETS and BIAS were computed at different mass mixing ratio thresholds (0.1, 0.3, 0.6, 1.0, 2.0, 3.0 g kg⁻¹) for the entire domain (D03) over the entire duration of the simulation.

The ETS in Clark et al. (2010) is calculated using four parameters, namely: “Hits” (the number of correct forecasts of occurrence), “Misses” (the number of occurrences which were missed by forecast), False Alarms (the number of false forecasts of nonoccurrence), and Correct Rejections (the number of correct forecasts of nonoccurrence), as below:

\[
ETS = \frac{Hits + Chance}{Hits + Misses + False Alarms - Chance}
\]

where,

\[
Chance = \frac{(Hits + False Alarms)(Hits + Misses)}{Hits + Misses + Correct Rejections}
\]

The ETS ranges between 0 and 1, where 0 indicates no skill, and 1 indicates perfect skill. The equation to compute the BIAS is:

\[
BIAS = \frac{Hits + False Alarms}{Hits + Misses}
\]

A BIAS above (below) 1, indicates that the algorithm over(under)-estimates the mass mixing ratios.

Before analyzing the quantitative evaluations of the retrievals, it is useful to re-iterate the major sources of the error in hydrometeor retrieval, namely: (i) The misidentification of the dominant hydrometeor type; (ii) the uncertainties in the assumed intercept parameters and bulk densities of hydrometeors, which were used in the Z0-q equations.

![Composite radar reflectivity fields of the true simulation on D03. The valid forecast time is shown above each panel.](image)
Fig. 5. Vertical cross-sections of the hydrometeor mixing ratio fields: $q_g$ (colour shadings), $q_s$ (blue contours), $q_r$ (green contours) from (a), (d) true simulation; (b), (e) $Z_h$T and (c), (f) FED-$Z_h$T. Legend for the colour shadings for $q_g$ ($g\ kg^{-1}$) is shown on the bottom. The contour intervals of $q_s$ ($g\ kg^{-1}$) are 0.1, 0.3, 1.0, 2.0, 4.0. The contour intervals of $q_r$ ($g\ kg^{-1}$) are 0.02, 0.5, 1.0, 2.0, 4.0. The locations of the vertical cross sections are denoted by the black lines in Fig. 4. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

Fig. 6. Vertical cross-sections of the biases in the retrievals of $q_g$ (colour shadings), $q_r$ (red and blue contours) relative to the true simulation values for (a), (c) $Z_h$T and (b), (d) FED-$Z_h$T. A positive value indicates overestimation, and vice versa. Legend for the colour shadings ($g\ kg^{-1}$) is shown on the bottom. Red solid (blue dash) contours denote positive (negative) values ($g\ kg^{-1}$) at intervals of ±0.3, ±1, ±2, ±3 respectively. The locations of the vertical cross sections are the same as in Fig. 5. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)
and (iii) the fraction assumptions of each class of hydrometeor in the mixed-hydrometeor regions (e.g., the mixed graupel/snow aggregates regions) in the retrieval method.

The retrievals of $q_g$ in FED-ZnT are associated with higher ETS compared to ZnT (Fig. 7a,d), which was traced back to FED-ZnT having more “Hits” and less “False Alarms” (not shown). The improvement was mainly seen for thresholds ranging between 0.1 and 0.6 g kg$^{-1}$, as the graupel particles, which have similar $Z_n$ to snow aggregates, typically have small $q_g$. A systematic underestimation of $q_g$ was still present in FED-ZnT, which could be caused by the uncertainties in the assumed intercept parameter and bulk density of graupel used in the $Z_q$ equation and the fraction assumptions. Compared with the retrievals of $q_g$ and $q_s$, the retrievals of $q_g$ exhibits relatively lower ETS at most thresholds in both methods (Fig. 7b,e), as more uncertainties existed in the PSD of snow aggregates (Zhang, 2016). The improvement of $q_g$ retrievals was mainly seen for thresholds exceeding 1 g kg$^{-1}$, as the snow aggregates, which have similar $Z_n$ to graupel particles, typically have large $q_g$.

For a given value of $Z_n$, snow aggregates exhibited a higher ice water content (IWC) than graupel, due to the differences in their respective PSDs. If graupel particles were mistakenly classified as snow aggregates (i.e., “Miss” event of graupel), the IWC would be overestimated, and vice versa. The BIAS of $q_g$ and $q_s$ (Fig. 7a,b,d,e) indicate that the FED-ZnT alleviated more “Misses” than “False Alarms” of graupel (what about $q_s$?). As a result, the overall IWC in the retrievals with ZnT were larger than those of FED-ZnT (not shown).

When assuming a variable $N_{ag}$, the ETS of $q_g$ was improved relative to the experiment using a constant $N_{ag}$. This improvement was mainly seen for thresholds above 0.6 g kg$^{-1}$ (Fig. 7c,f). The $q_g$ above 0.6 g kg$^{-1}$ was systematically overestimated with ZnT, while such overestimation was reduced in FED-ZnT.

### 4.2. Short-term forecasts with the data assimilation of hydrometeor retrievals

To test the effects of the improved hydrometeor retrievals on the short-term forecast of the MCS, the hydrometeor retrievals using ZnT and FED-ZnT were respectively assimilated into the model using the NCAR WRF-RTFDDA system. This data assimilation (DA) tool makes use of Newtonian relaxation nudging based on four-dimensional data DA. There are two types of DA methods currently implemented in WRF-RTFDDA (Stauffer and Seaman, 1990; Liu et al., 2006): the observation nudging and grid nudging. The grid nudging method was designed to assimilate three-dimensional data with high temporal-spatial resolution. In the grid nudging, background fields are nudged toward the observations/analyses at the corresponding analysis-model grid points, following Eq. (6):

$$\frac{\partial X}{\partial t} = P(X, t) + G_t \cdot T_v \cdot (Y_t - X_t)$$

where $X_t$ is the model-state variable, $P(X, t)$ is the model original prognostic equation, $G_t$ is the relaxation time scale used to reduce noise induced by instantaneous change of the model fields, $T_v$ is a time weight, which is a function of the time lags between the observation and model state, $Y_t$ is the observation or analysis value on the model grids.

When assimilating the mixing ratio of each class of the hydrometeor, the corresponding latent heat releases were also computed and assimilated into the model using the latent heat nudging module of WRF-RTFDDA.

The true simulation used here was the same as in Section 2.2. The configurations of the control (no DA) and the DA experiment were the same as in the true simulation except for the initial conditions. The initial conditions of the control and the DA run were generated by randomly perturbing the ERA-Interim reanalysis at the initial time. The perturbations were obtained by a stochastic sampling the background error covariance from the WRF-DA (Barker et al., 2004), and were applied to the air temperature, wind, and water vapor. The descriptions and acronyms of all the experiments are summarized in Table 2. In ASML-ZnT and ASML-FzT, the hydrometeor retrievals were continuously assimilated in the innermost domain for 2-h from the initialization of that domain at 0900 UTC. From the end of the analysis at 1100 UTC, 4-h forecasts were performed in each experiment.

Since precipitation is an accumulated field, while radar reflectivity is instantaneous, it is expected that precipitation will be more sensitive to the analysis of hydrometeor fields compared to radar reflectivity. Therefore, the hourly precipitation for each experiment was analyzed (Fig. 8). Overall, both assimilation experiments (i.e., ASML-ZnT and
ASML-FZhT performed better than CTRL, indicating that assimilating the observation-based hydrometeor retrievals can improve short-term precipitation forecast of this MCS. The displacement errors in CTRL were reduced in the assimilation experiments. The areal coverage of the MCS was smaller in CTRL. The northwestern portion of the precipitation field of the MCS was absent in CTRL (Fig. 8a,b,e,f), due to weak temperature gradients coupled with, marginal convergence there (Fig. 9b). In the assimilation experiments, appreciable updrafts were induced in those regions through latent heat nudging (Fig. 10c). The assimilated hydrometeors produced more rainfall there, which resulted

<table>
<thead>
<tr>
<th>Experiment names</th>
<th>Initial condition</th>
<th>Data used for hydrometeor retrieval</th>
<th>Descriptions</th>
</tr>
</thead>
<tbody>
<tr>
<td>TRUE</td>
<td>ERA-Interim reanalysis</td>
<td>\</td>
<td>True simulation</td>
</tr>
<tr>
<td>CTRL</td>
<td>ERA-Interim reanalysis with a random perturbation \</td>
<td>Zth, T</td>
<td>Control run without data assimilation</td>
</tr>
<tr>
<td>ASML-ZthT</td>
<td>The same as in CTRL</td>
<td>Zth, T</td>
<td>Data assimilation run using the hydrometeor retrievals from Zth and T</td>
</tr>
<tr>
<td>ASML-FZhT</td>
<td>The same as in CTRL</td>
<td>FED, Zth, T</td>
<td>Data assimilation run using the hydrometeor retrievals from FED, Zth and T</td>
</tr>
</tbody>
</table>

**Fig. 8.** Hourly accumulated precipitation rates (mm) for (a), (e), (i): TRUE; (b), (f), (j): CTRL; (c), (g), (k): ASML-ZthT; and (d), (h), (l): ASML-FZhT. The valid forecast time is shown above each panel with 0-h representing the last hour of the analysis time.
in a stronger cool pool and outflow front (Fig. 9c,d). The outflow front continuously lifted the warmer and moister air ahead of it, sustaining convection there. During the forecast, both assimilation experiments exhibit weaker rainfall amounts relative to the true simulation to the southwest, but have larger rainfall to the northeast (Fig. 8i,k,l). This could be explained by the humidity field in the initial conditions (Fig. 10): by the end of the analysis time, the air ahead of the southwest portion of the MSC was drier in the assimilation experiments than in the true simulation, while the air ahead of the northeast portion of the MSC was moister in the assimilation experiments compared to the true simulation (Fig. 10a,c). These humidity biases at larger scales did have a pronounced effect on the accumulated precipitation forecasts in the assimilation experiments.

In the analysis period, the morphology and location of the MCS in ASML-FZhT were similar to those of ASML-ZhT. The convective precipitation of ASML-ZhT, however, was stronger than in ASML-FZhT and presented a larger bias than ASML-FZhT when taking the true simulation as the reference (Fig. 8a,c,d). This was partly due to the analysis fields in ASML-ZhT exhibiting higher LWC and IWC, as explained in Section 3.1. Additionally, the latent heat releases were proportional to the increments of LWC and IWC, which resulted in larger temperature increments in ASML-ZhT, and a correspondingly stronger thermodynamic forcing. Other background fields would also be adjusted through the kinematic and microphysics to accommodate the changes in thermodynamic forcing. Compared to ASML-ZhT, the convective region of the analysis fields in ASML-FZhT contained more graupel, which was more prone to precipitate than snow aggregate. Snow aggregate, however, could gradually undergo riming wherever supercooled water subsisted, to eventually convert into graupel. In summary, ASML-ZhT could produce more precipitable ice due to the overestimation of the IWC and the gradual riming of snow aggregates.

During the forecast period, although the hydrometeor analyses were no longer assimilated, ASML-ZhT still produced heavier rainfall and larger rainfall maxima than ASML-FZhT and TRUE (Fig. 8e-l). This could be explained by the stronger cold pool and gust front in ASML-ZhT (Fig. 8c,d), which were associated with heavier precipitation in the
analysis period, and, thus, deeper cold pool (e.g., Gilmore and Wicker, 1998; Fierro et al., 2008). The strengthening of the initial cold pool yielded a positive feedback with the precipitation fields (Fig. 9g,h).

To quantitatively compare the precipitation forecast of different experiments, the Fractions Skill Score (FSS, Roberts and Lean, 2008) at different thresholds and different neighborhood radii from 1 to 30 km (i.e., 1–30 neighborhood grid cells) were calculated for hourly-accumulated precipitation forecasts for each experiment. Since the FSS is more tolerant to small displacement errors compared to the ETS, it is more appropriate for the evaluation of the simulation with fine resolution grids (e.g., Fierro et al., 2015). The precipitation from the true simulation was regarded as the reference when computing the FSS for each experiment. For the sake of brevity, only the results for the 15- km neighborhood radius at the rainfall thresholds of 2.5 and 10 mm were presented herein (Fig. 11). In general, the assimilation experiments (i.e., ASML-Z_T, ASML-FZ_T) achieved higher FSS compared to CTRL at all thresholds in both the analysis and forecast periods (Fig. 11). CTRL produced a low FSS, due to the large displacement errors of the simulated MCS, as well as the selected small neighborhood radius for the FSS computation. The more accurate analysis of the hydrometeor fields in ASML-FZ_T resulted in slightly higher FSS compared with ASML-Z_T. The improvement was clearer at the threshold of 10 mm (Fig. 11b) compared to 2.5 mm (Fig. 11a), indicating the improvement of hydrometeor analysis had more impact on the forecast of convective precipitation than those of stratiform precipitation.

5. Conclusions

This study presents a hydrometeor retrieval method, which combines S-band Z_R, T and FED data. The hydrometeor retrieval method is based on those proposed by Lerach et al. (2010), Gao and Stensrud (2012) and Pan et al. (2016), who employed S-band Z_R and ambient T to retrieve hydrometeors. Since the ranges of Z_R of graupel and snow aggregates are partially overlapping, uncertainties exist in distinguishing the graupel-dominated and snow aggregates-dominated regions when only using Z_R and T data. The hydrometeor retrieval method presented in this study incorporates lightning data into the Z_R and T based hydrometeor retrieval algorithm. Lightning data are utilized to better discern regions containing graupel in clouds. Different Z_R thresholds are then applied to different regions to identify the graupel-dominated and snow aggregates-dominated regions. For the quantitative estimation of q_v, different N_{th} are used for different ranges of Z_R and different estimated precursors of raindrop in cold-cloud microphysical processes (i.e., graupel or snow aggregate).

The hydrometeor retrieval method was tested with the observing system simulation experiment (OSSE) in which the input data for the hydrometeor retrieval (i.e., the FED, Z_R and T data) were obtained from a MCS simulation using explicit electrification implemented in the WRF model, which couples an explicit charging and bulk discharge lightning scheme in the NSSL double-moment microphysics, at cloud-resolving scale (1-km). By incorporating the FED as additional input data source into the Z_R and T based hydrometeor retrieval method, the hydrometeor retrieval accuracy was improved. However, uncertainties still existed in the quantitative retrieval of hydrometeor mixing ratio, which primarily arise from the assumptions behind the hydrometeor PSD and the fraction of each class of hydrometeor in the mixed-hydrometeor regions. The graupel PSD may evolve in response to changing lightning rate, as both the graupel PSD and total lightning rate are related to the updraft strength. For example, decreasing total lightning rate may indicate the decrease of updraft strength, which may shift the peak of the graupel PSD toward the smaller particles. The relationship between graupel PSD and total lightning rate could be incorporated into the lightning data based-hydrometeor retrieval method when such relationships are better understood, which remains the subject of future research endeavors.

The hydrometeor retrievals (with and without lightning information) were respectively assimilated into WRF using the NCAR-RTFDDA assimilation and forecast system. Both of the assimilation experiments performed better than the control experiment. Assimilating the hydrometeor retrievals with the added information from lightning slightly improved the analyses and forecasts of precipitation in a test MCS case. Overall, the improvement was more pronounced for the convective precipitation. The improvement could be due to the more accurate hydrometeor analysis, which further affected the strength of cold pool and gust front. The cold pool and gust front feedbacked with the subsequent evolution of MCS by impacting the storm thermodynamic environment. Because the evolution of convective systems is affected by complex nonlinear processes, future research should be devoted to the testing and evaluation of additional cases, preferably spanning different regimes.

The current lightning-based hydrometeor retrieval method is not expected to serve as a surrogate for hydrometeor retrieval methods based on polarimetric radar, which contains a larger wealth of information to infer the characteristics of hydrometeor species. For instance, when using polarimetric radar based hydrometeor retrieval method, Z_{DR} above 0 °C can be used to indicate the existence of supercooled raindrops (e.g., Kumjian and Ryzhkov, 2008); Z_{DR} and K_{DP} can be used to estimate the Z_R associated with rain and perceptible ice particles in the mixed-phase region, respectively, (e.g., Carey and Rutledge, 2000). Achieving such level of detail is beyond the capabilities of the current lightning-based hydrometeor retrieval method. Until present, however, most of the operational weather radars in China have not yet been upgraded to polarimetric technology, and under the circumstances that the real-time nationwide detection of lightning will be provided by the recently-launched FY-4 geostationary satellite, it is expected that incorporating total lightning data into the non-polarimetric radar-based hydrometeor retrieval methods could add value to the hydrometeor retrieval and short-term forecast of MCS at small additional expenses. Because only case was analyzed with an OSSE, this study should be viewed as a “proof-of-concept” for a tentative lightning based hydrometeor retrieval method. Consequently, the applicability of
this method to realistic settings (i.e., non-OSSE) requires further testing with real observation data, namely: the FED data from the FY-4 geostationary satellite, dual-polarimetric radar data, and other surface based datasets.

Acknowledgments

This work was supported by the State Grid Corporation of China under the Sciences and Technology Project: SGTYHT/14-JS-188, the Postgraduate Research and Innovation Projects of Jiangsu Province: KYLX16_0939, the National Key Basic Research Program of China: Grant No. 2014CB441043. We would like to acknowledge high-performance computing support from Yellowstone (ark:/85065/d7w3x3hc) provided by NCAR’s Computational and Information Systems Laboratory, sponsored by the National Science Foundation. ERA-Interim data provided courtesy ECMWF.

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